

# Representative use cases and performance trade-offs

**Daniel Bonilla Licea**<sup>1</sup>, Giuseppe Silano<sup>3,2</sup>, Hajar El Hammouti<sup>1</sup>, Martin Saska<sup>2</sup>, and Mounir Ghogho<sup>1</sup>

Half-day Tutorial Session at ICUAS 2026 (09:00 – 13:00), 15<sup>th</sup> June 2026  
Room Calypso A – Divani Corfu Palace

<sup>1</sup>Mohammed VI Polytechnic University, Ben Guerir, Morocco,

<sup>2</sup>Czech Technical University in Prague, Prague, Czechia,

<sup>3</sup>Ricerca sul Sistema Energetico, Milan, Italy

daniel.bonilla@um6p.ma



# Case 1: Energy efficiency

A **quadrotor** must go **from a starting point to a goal point** while transmitting as much data as possible to a base station, using as little energy as possible. This must be done in a **finite time  $T$** .



## Problem Formulation

minimize  $J(\mathcal{C}, \mathcal{T})$   
s.t. **Motion model,**  
**Channel model,**  
**Trajectory constraints,**  
**Communication constraints.**

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## Problem Formulation

$$\begin{aligned} & \underset{\mathcal{C}, \mathcal{T}}{\text{minimize}} && J(\mathcal{C}, \mathcal{T}) \\ & \text{s.t.} && \dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}), \\ & && \text{Channel model,} \\ & && \mathbf{x}(T) = \mathbf{x}_g, \\ & && \text{Communication constraints.} \end{aligned}$$

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Should we consider:

- **ONLY** the energy spent by the motors?
- **ALSO** the energy spent by the transmitter?

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In this example, we take  $E(0, T) = f_{\text{mech}}(\mathcal{T})$ .

How to include  $E(0, T)$  into the optimization problem?

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Depending on prior information:

- **STOCHASTIC** model. (almost none)
- **MEASUREMENT** based model. (RF measurements at some positions)
- **RAY TRACING** model. (3D map)

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Stochastic model with shadowing.

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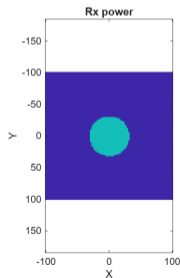
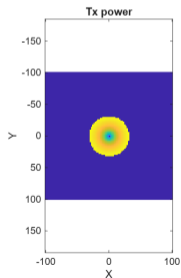
Does the transmitter use:

- Power control?
- Constant power?

# Case 1: Energy efficiency

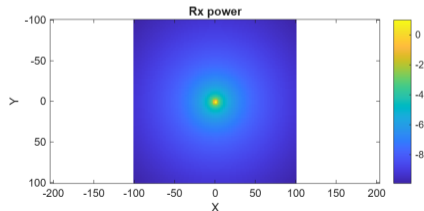
## Power control

- $P_{\text{ref}}$  at the receiver whenever possible.
- Requires feedback for channel estimation.
- Transmitted data **depends on time** spent in connected regions.



## Constant power

- Transmits with constant power, received power depends on transmitter position.
- No feedback required.
- Transmitted data **depends on trajectory**.



**BOTH MECHANISMS LEAD TO DIFFERENT PROBLEMS**

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For constant tx power the tx rate is

$$r(t) = B \log_2 \left( 1 + \frac{h^2(\mathbf{p})P}{\|\mathbf{p}_{rx} - \mathbf{p}_{tx}\|^2 \sigma_n^2} \right)$$

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$$r(t)$$

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- How to include  $E(0, T)$ ?
- How to include  $r(t)$ ?
- How to combine  $E(0, T)$  and  $r(t)$ ?

# Case 1: Energy efficiency

OP 1

$$\begin{aligned} & \underset{\mathbf{u}}{\text{maximize}} && \frac{\int_0^T r(t) dt}{E(0, T)} \\ & \text{s.t.} && \dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}), \\ & && y(t) = \frac{h(\mathbf{p})s(t)}{\|\mathbf{p}_{rx} - \mathbf{p}_{tx}\|} + n_{rx}(t), \\ & && \mathbf{x}(T) = \mathbf{x}_g, \end{aligned}$$

OP 2

$$\begin{aligned} & \underset{\mathbf{u}, E_{max}}{\text{maximize}} && \int_0^T r(t) dt - E_{max} \\ & \text{s.t.} && \dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}), \\ & && y(t) = \frac{h(\mathbf{p})s(t)}{\|\mathbf{p}_{rx} - \mathbf{p}_{tx}\|} + n_{rx}(t), \\ & && \mathbf{x}(T) = \mathbf{x}_g, \\ & && E(0, T) < E_{max}. \end{aligned}$$

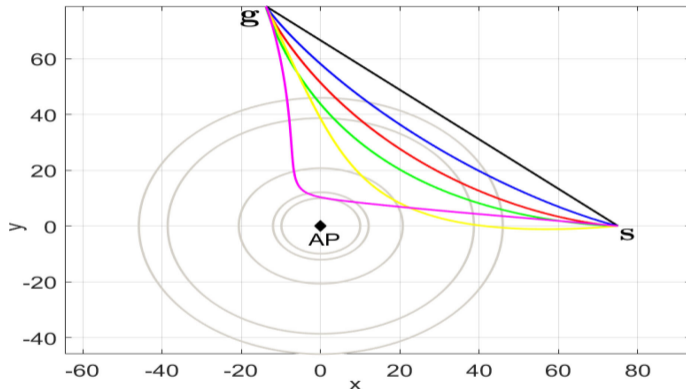
OP 3

$$\begin{aligned} & \underset{\mathbf{u}}{\text{minimize}} && \vartheta E(0, T) + (1 - \vartheta) \left( \int_0^T r(t) dt \right)^{-1} \\ & \text{s.t.} && \dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}), \\ & && y(t) = \frac{h(\mathbf{p})s(t)}{\|\mathbf{p}_{rx} - \mathbf{p}_{tx}\|} + n_{rx}(t), \\ & && \mathbf{x}(T) = \mathbf{x}_g, \end{aligned}$$

OP 4

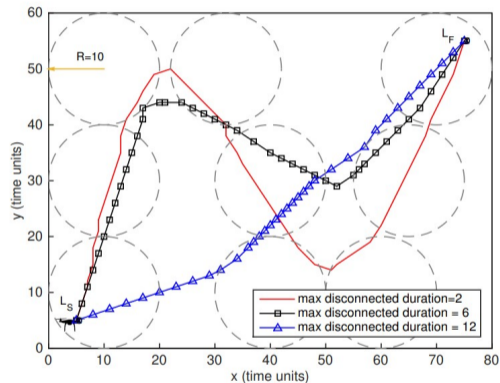
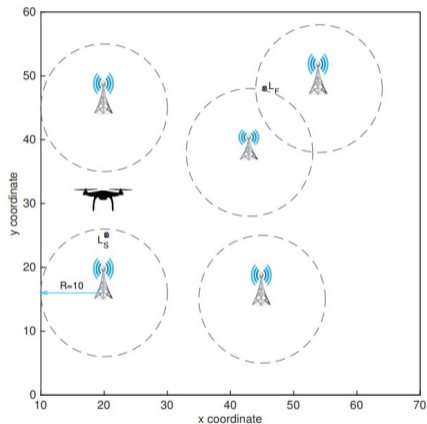
$$\begin{aligned} & \underset{\mathbf{u}, D}{\text{minimize}} && E(0, T) + D^{-1} \\ & \text{s.t.} && \dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u}), \\ & && y(t) = \frac{h(\mathbf{p})s(t)}{\|\mathbf{p}_{rx} - \mathbf{p}_{tx}\|} + n_{rx}(t), \\ & && \mathbf{x}(T) = \mathbf{x}_g, \\ & && \int_0^T r(t) dt > D. \end{aligned}$$

# Case 1: Energy efficiency



D. Bonilla Licea, et al., “*Communication-Aware Energy Efficient Trajectory Planning With Limited Channel Knowledge,*” in IEEE Transactions on Robotics, 2020

## Case 2: Disconnectivity



E. Bulut et al, "Trajectory Optimization for Cellular-Connected UAVs with Disconnectivity Constraint," in IEEE International Conference on Communications Workshops, 2018.

# Thank you

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